

# 14.452 Recitation 1

Panel Data, Democracy, Kaldor

Todd Lensman

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These slides build on work by past 14.452 TAs: Shinnosuke Kikuchi, Joel Flynn, Karthik Sastry, Ernest Liu, Ludwig Straub, . . .

- ▶ Welcome to 14.452!
  - ▶ great class for thinking rigorously about **big** questions
  - ▶ useful to see this material even if you're not into macro
  - ▶ lots of information/literature/models – try to keep the big picture in mind
- ▶ Recitation: Friday 2:30p-4p, E51-151 (exception: week of November 14)
- ▶ Office hours: Tuesday 10:30a-11:30a **and** 2:30p-4:00p, E52-548
- ▶ Email: [tlensman@mit.edu](mailto:tlensman@mit.edu)
- ▶ Problem sets due at 2:30p on Friday

## Recitations

- ▶ Please interrupt with any questions or comments
- ▶ Based on popular demand I will prioritize:
  1. practice problems related to the lectures/problem sets/exam
  2. review of lecture material
  3. open Q&A
  4. new paper discussion
- ▶ Slides posted online before recitations
- ▶ Let me know if this works for you – happy to adjust!

## Plan for today

### 1. Intro to panel data

- ▶ application to democracy and growth

### 2. Reviewing the Kaldor facts

- ▶ closer look at factor shares
- ▶ detour: elasticity of substitution

# Panel Data, Democracy, and Growth

## Setting

- ▶  $c \in \{1, \dots, N\}$ : cross-section (*countries*)
- ▶  $t \in \{1, \dots, T\}$ : time-series (*years*)
- ▶  $y_{ct}$ : outcome (*per capita GDP*)
- ▶  $D_{ct}$ : treatment (*democracy*)
- ▶ **Question:** what is the causal effect of  $D_{ct}$  on  $y_{ct}$ ?
  - ▶ when could we identify such a causal effect, even though we aren't doing a proper laboratory experiment?

$$y_{ct} = \delta_c + \gamma_t + \alpha D_{ct} + \varepsilon_{ct}$$

### Why did we write this down?

- ▶  $\delta_c$ : country fixed effect
  - ▶ countries have *constant* characteristics over time
  - ▶ characteristics have *constant* effect on output
- ▶  $\gamma_t$ : time fixed effect
  - ▶ aggregate shocks with *uniform* effects on the whole world
- ▶  $\alpha D_{ct}$ : coefficient of interest
  - ▶ democracy has the *same* impact on growth in all countries
- ▶  $\varepsilon_{ct}$ : residual
  - ▶ everything we forgot about!
  - ▶ education, health, capital, weather, ...

## Fixed effects and identification

- ▶ What happens if we just regress  $y_{ct}$  on  $D_{ct}$ ?

$$y_{ct} = \alpha D_{ct} + u_{ct}$$

- ▶ What **story** undermines the regression?
  - ▶ “highly educated countries have high  $\delta_c$  and more democracy. The correlation of democracy and output picks this up, even if democracy has a negative or zero effect on growth”
- ▶ Math version:  $\text{Cov}[D_{ct}, u_{ct}] > 0$

$$\hat{\alpha} = \alpha + \frac{\hat{\text{Cov}}[D_{ct}, u_{ct}]}{\hat{\text{Var}}[D_{ct}]} > \alpha$$



## Estimating fixed effects

- ▶ Let's estimate the regression with fixed effects
  - ▶ mechanics: include dummy variables for each country

- ▶ **Theorem (Frisch-Waugh)**: same as de-meaning each country:

$$(y_{ct} - \hat{\mathbb{E}}_t y_{ct}) = \alpha(D_{ct} - \hat{\mathbb{E}}_t D_{ct}) + (\gamma_t - \hat{\mathbb{E}}_t \gamma_t) + (\varepsilon_{ct} - \hat{\mathbb{E}}_t \varepsilon_{ct})$$

- ▶  $\hat{\mathbb{E}}_t$  sample average w.r.t time  $t$
  - ▶ does an increase of democracy *within* a country affect growth?
  - ▶ countries with  $D_{ct} \neq D_{ct'}$  identify  $\alpha$
  - ▶ countries with  $D_{ct}$  fixed help to estimate  $\gamma_t$
- ▶ Often called a “within estimator” because uses “within-country” variation

## Strict exogeneity: the gold standard

- ▶ What assumption do we need for OLS to give unbiased estimates?
- ▶ Informally, need democracy at  $t$  to be uncorrelated with all past and future shocks to GDP
- ▶ This is implied by the usual assumption of *strict exogeneity*:

$$\mathbb{E}[\varepsilon_{ct} | \delta_c, (\gamma_s, D_{cs})_{s=1}^T] = 0, \quad \forall t \in \{1, \dots, T\}$$

- ▶ Note that this is stronger than the typical conditional mean independence assumption in cross-sectional regressions (need to estimate the  $c$  fixed effects)

## First differences

- ▶ What if we estimated in first differences to remove the  $\delta_c$ ?

$$y_{ct} - y_{ct-1} = \alpha (D_{ct} - D_{ct-1}) + \gamma_t - \gamma_{t-1} + \varepsilon_{ct} - \varepsilon_{ct-1}$$

- ▶ This works, with the new identifying assumption

$$\mathbb{E}[(D_{ct} - D_{ct-1})(\varepsilon_{ct} - \varepsilon_{ct-1}) | \gamma_t - \gamma_{t-1}] = 0.$$

- ▶ Hard to find examples where this would hold but strict exogeneity doesn't (what's so special about last year?)

## Lags and identification

- ▶ What if democracy (and output) respond to previous shocks?
- ▶ Motivates including lagged  $y_{ct}$  or  $\Delta y_{ct}$  on the right-hand-side, e.g.

$$y_{ct} = \delta_c + \gamma_t + \alpha D_{ct} + \rho y_{ct-1} + \varepsilon_{ct}$$

- ▶ Does strict exogeneity still make sense? **No!**  
→ if  $\rho > 0$ ,  $\varepsilon_{ct}$  must be correlated with regressors at  $s \geq t + 1$
- ▶ Informal identification condition:

$$\begin{aligned} \{D_{ct}, \text{ not predicted by lag GDP}\} &= \text{“Good variation in } D_{ct}\text{”} \\ &= \text{“As good as random”} \end{aligned}$$

- ▶ What exogeneity assumption makes sense in this case?

**PS1 Question** – check out “*Democracy Does Cause Growth*”

## Results

	log GDP	GDP growth	log GDP		
	(1)	(2)	(3)	(4)	(5)
Democracy	-10.112** (4.32)	1.276*** (0.31)	0.973*** (0.29)	0.651*** (0.25)	0.794*** (0.22)
log GDP (-1)			0.973*** (0.01)	1.266*** (0.04)	1.245*** (0.04)
log GDP (-2)				-0.300*** (0.04)	-0.211*** (0.05)
log GDP (-3)					-0.069*** (0.02)
Year FE	Yes	Yes	Yes	Yes	Yes
Country FE	Yes	Yes	Yes	Yes	Yes
Observations	6934	6790	6790	6642	6490
R-squared	0.970	0.157	0.999	0.999	0.999

**Table 1:** Regression results. *Notes:* Standard errors clustered at the country level. \*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

## Nickell (1981) bias

- ▶ New econometric issues come up when including lagged outcome variables as regressors
- ▶ Nickell (1981): typical “within” estimator is biased for finite  $T$
- ▶ This again follows from the failure of strict exogeneity:

$$\mathbb{E} \left[ \left( y_{ct-1} - \hat{\mathbb{E}}_t y_{ct-1} \right) \left( \varepsilon_{ct} - \hat{\mathbb{E}}_t \varepsilon_{ct} \right) \right] \neq 0$$

- ▶ There are ways to deal with this bias, e.g. using GMM (Arellano & Bond 1991)
- ▶ Upshot: generally don't want to use OLS unless  $T$  is large

## Kaldor Facts and Changing Factor Shares

## What are the facts?

Kaldor, Nicholas (1957): “A Model of Economic Growth”

- (i) Constant shares of national income to capital and labor
- (ii) Constant growth of capital per worker
- (iii) Constant growth of output per worker
- (iv) Constant capital to output ratio
- (v) Constant return on investment
- (vi) There exist “acceptable” 2-5 percent variations in labor productivity growth across countries

We use these to define “balanced growth,” but are they (still) true?



## Factor shares with Cobb-Douglas production

- ▶ Suppose a Cobb-Douglas production function:

$$Y = F(K, L) = AK^\alpha L^{1-\alpha}$$

- ▶ Assuming markets are competitive, what share of output  $s_L$  is paid to workers?  
First find the wage:

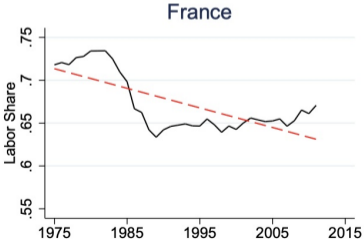
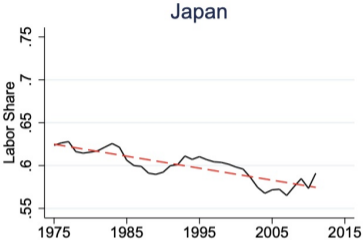
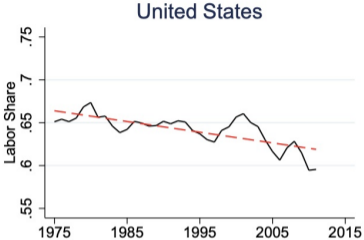
$$w = F_L(K, L) = (1 - \alpha)AK^\alpha L^{-\alpha} = (1 - \alpha)\frac{Y}{L}$$

- ▶ Rearrange:

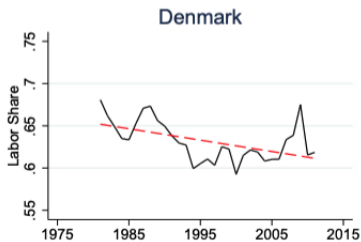
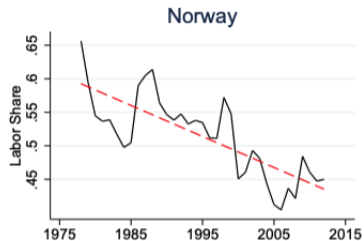
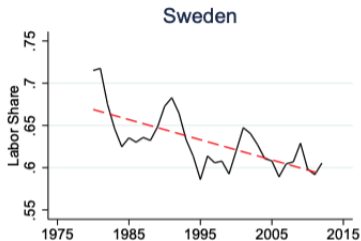
$$s_L = \frac{wL}{Y} = 1 - \alpha$$

- ▶ With Cobb-Douglas, factor shares are **constant** (indep. of prices/quantities)
- ▶ Is this true in the data?

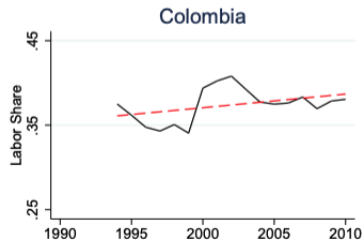
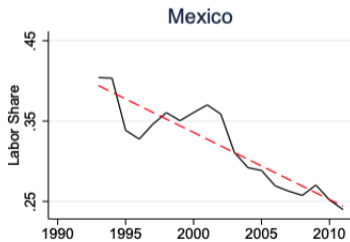
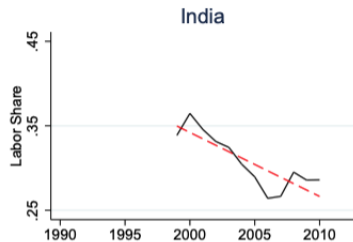
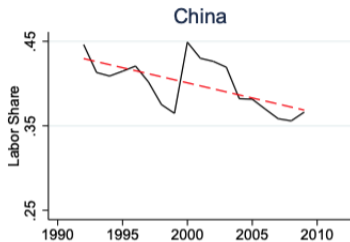
# Advanced countries (Karabarbounis and Neiman 2014)



## Other advanced countries (Karabarbounis and Neiman 2014)



# Developing countries (Karabarbounis and Neiman 2014)



## Many (potential) explanations

- ▶ Decrease in price of capital
- ▶ Superstar firms with low labor shares/ICT
- ▶ Automation
- ▶ China shock
- ▶ Labor market imperfections/regulations
- ▶ Accounting/mechanical reasons
  - ▶ intellectual property product capitalization
  - ▶ housing treatment
  - ▶ “profit share”

Grossman & Oberfield (2022): “The Elusive Explanation for the Declining Labor Share”

## Falling capital price (Karabarbounis and Neiman 2014)

- ▶ Idea: fall in the price of capital  $R$  ( $\approx$  productivity improvements in IT/computers) drives substitution away from labor and toward capital
- ▶ But even if  $K/Y$  increases (**quantity effect**), still have falling  $R$  (**price effect**)  
 $\Rightarrow$  change in capital share  $s_K = RK/Y$  is indeterminate
- ▶ *Didn't we just show that factor shares don't depend on prices anyway?*
- ▶ Yes, but only for Cobb-Douglas  
 $\rightarrow$  too restrictive for thinking about the effects of prices on income shares

## Beyond Cobb-Douglas: constant elasticity of substitution (CES)

- ▶ Arrow, Chenery, Minhas, & Solow (1961) introduce CES production:

$$F(K, L) = \left[ \alpha (A_K K)^{\frac{\sigma-1}{\sigma}} + (1 - \alpha) (A_L L)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

- ▶  $A_K, A_L$  factor-augmenting productivities
  - ▶  $\alpha$  share parameter
  - ▶  $\sigma$  (constant) **elasticity of substitution**
- ▶ Looks messy, but learn to love it (at least in macro)

## Why CES?

$$F(K, L) = \left[ \alpha (A_K K)^{\frac{\sigma-1}{\sigma}} + (1 - \alpha) (A_L L)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

### 1. Nice special cases

**Perfect Complements** as  $\sigma \rightarrow 0$ :

$$F(K, L) \rightarrow \min \left\{ \frac{A_K K}{\alpha}, \frac{A_L L}{1 - \alpha} \right\}$$

**Cobb-Douglas** as  $\sigma \rightarrow 1$ :

$$F(K, L) \rightarrow (A_K K)^\alpha (A_L L)^{1-\alpha}$$

**Perfect Substitutes** as  $\sigma \rightarrow \infty$ :

$$F(K, L) = \alpha A_K K + (1 - \alpha) A_L L$$



## Why CES?

$$F(K, L) = \left[ \alpha (A_K K)^{\frac{\sigma-1}{\sigma}} + (1-\alpha) (A_L L)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

2. Unit cost function (**price index**) is also CES with elasticity  $1/\sigma$ :

$$P = c(R, w) = \left[ \alpha^\sigma \left( \frac{R}{A_K} \right)^{1-\sigma} + (1-\alpha)^\sigma \left( \frac{w}{A_L} \right)^{1-\sigma} \right]^{\frac{1}{1-\sigma}}$$

## Why CES?

$$F(K, L) = \left[ \alpha (A_K K)^{\frac{\sigma-1}{\sigma}} + (1 - \alpha) (A_L L)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

### 3. Convenient factor shares that *depend on prices!*

$$\frac{s_K}{1 - s_K} = \frac{\frac{RK}{Y}}{\frac{wL}{Y}} = \left( \frac{\alpha}{1 - \alpha} \right)^{\sigma} \left( \frac{R/A_K}{w/A_L} \right)^{1-\sigma}$$

- ▶ capital share decreasing in relative capital price  $\iff \sigma > 1$
- ▶ price effect dominates for  $\sigma < 1$ , quantity effect dominates for  $\sigma > 1$

## Back to falling capital prices

- ▶ With more flexible (CES) substitution, can a decline in the relative price of capital  $R/w$  explain the decline in the labor share  $s_L$ ?
  - only if  $\sigma > 1$  (capital and labor are substitutes)
- ▶ Oberfield & Raval (2021): “Micro Data and Macro Technology”
  - $\sigma$  around 0.5 – 0.7 in US manufacturing sector
- ▶ Falling capital price probably isn't the explanation!

## One last thing...

- ▶ But what is  $\sigma$ ? More generally, what is an elasticity of substitution (EoS)?
- ▶ For **homothetic** production function  $F(K, L)$ , EoS measures the curvature of an isoquant:

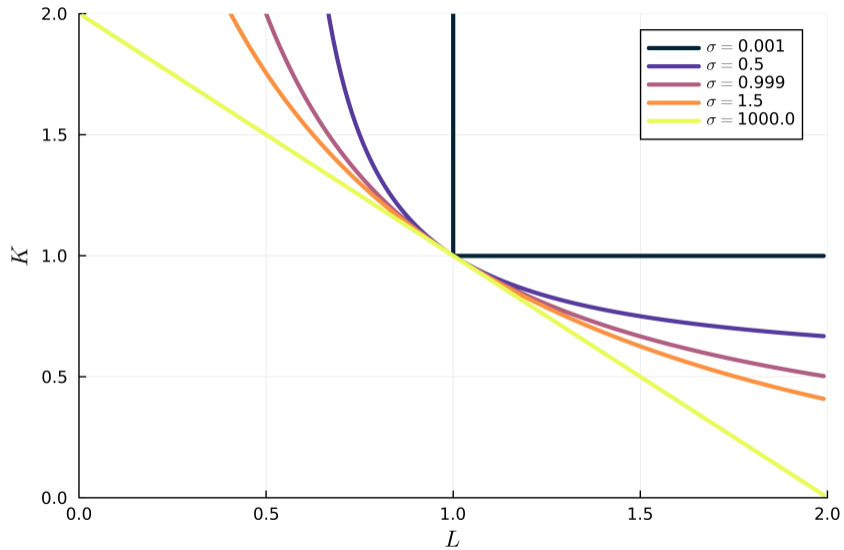
$$\frac{1}{EoS\left(\frac{K}{L}\right)} = -\frac{\partial \log\left(\frac{F_K}{F_L}\right)}{\partial \log\left(\frac{K}{L}\right)}$$

- ▶ higher EoS  $\Rightarrow$  “flatter” isoquant  $\Rightarrow$   $K, L$  “more substitutable”
- ▶ Equivalently, EoS measures change in cost-minimizing input ratio w.r.t. price ratio:

$$EoS\left(\frac{r}{w}\right) = -\frac{\partial \log\left(\frac{K}{L}\right)}{\partial \log\left(\frac{r}{w}\right)}$$

- ▶ CES  $F$  is the **unique**  $F$  with EoS independent of quantities (or prices)
- ▶ Lots of other concepts of EoS when production function has  $\geq 3$  inputs  
Allen-Uzawa, Morishima, ...

## CES in a figure



Questions?